Stochastically timed predicate-based communication primitives for autonomic computing

Diego Latella
ISTI - CNR

Michele Loreti
Università di Firenze

Mieke Massink
ISTI - CNR

Valerio Senni
IMT Lucca

Predicate-based communication allows components of a system to send messages and requests to ensembles of components that are determined at execution time through the evaluation of a predicate, in a multicast fashion. Predicate-based communication can greatly simplify the programming of autonomous and adaptive systems. We present a stochastically timed extension of the Software Component Ensemble Language (SCEL) that was introduced in previous work. Such an extension raises a number of non-trivial design and formal semantics issues with different options as possible solutions at different levels of abstraction. We discuss four of these options, of which two in more detail. We provide a formal semantics and an illustration of the use of the language modeling a variant of a bike sharing system, together with some preliminary analysis of the system performance.

1 Introduction

The next generation of software-intensive distributed computing systems has to deal with issues that arise from the presence of possibly large numbers of heterogeneous components, featuring complex interactions, and operating in open and non-deterministic environments. A further challenge is to deal with dynamic adaptation as response to evolving requirements and changes in the working environment [12, 13, 18]. Applications with the above characteristics are already being built and can be found in, for example, smart spaces, sensor networks, and large online cloud systems. Devising appropriate abstractions and linguistic primitives together with a consistent programming methodology is essential for the structured and reliable design of these complex systems. One proposal that has been put forward to this aim is the notion of ensemble, and in particular that of autonomic service components (AC) and autonomic service-component ensembles (ACE). The former are autonomic entities whereas the latter are collections of ACs with dedicated knowledge units and resources, and with a goal-oriented execution. Both notions play a central role in the recently developed kernel language SCEL (Software Component Ensemble Language) [4, 7] together with a number of abstractions that are specifically designed for representing behaviours, knowledge, and aggregations according to specific policies, and to support programming context-awareness, self-awareness, and dynamic adaptation.

Two novel key aspects of SCEL, that distinguish it from other languages, are designed to support the development of autonomous, loosely-coupled, component-based software systems: predicate-based communication and the component knowledge-base. Predicate-based communication allows to send messages to ensembles of components that are not predetermined at modeling time, but are defined at execution time, depending on how the communication predicate evaluates w.r.t. the receiver interface. The component knowledge-base provides the realisation of various adaptation patterns, by explicit separation of adaptation data in the spirit of [3], and to model the components view on (and awareness of) the environment. SCEL has been used to specify many scenarios related to the Case Studies of the ASCENS project [8]. These specifications witness how SCEL primitives simplify the programming of autonomous and adaptive systems.
In this paper we address the problem of enriching SCEL with information about action duration by providing a stochastic semantics for the language. Such a semantics is important for the analysis of the performance aspects of ensemble based systems. There exist various frameworks that support the systematic development of stochastic languages, such as [6]. However, the main challenge in developing a stochastic semantics for SCEL is in making appropriate modeling choices, both taking into account the specific application needs and allowing to manage model complexity and size. The main contribution in this work is the proposal of four variants of STOCS, a Markovian extension of a significant fragment of SCEL, that can be used to support quantitative analysis of adaptive systems composed of ensembles of cooperating components. Providing suitable Markovian semantics to predicate based ensemble languages poses a number of design challenges regarding the temporal ordering of multicast and information request actions that differ considerably from traditional process algebras. The four variants adopt the same language syntax of SCEL, or restrictions thereof, but denote different underlying stochastic models, having a different level of granularity. We obtain these variants by modifying labels and relations used to construct the transition systems.

Finally, an important aspect in a modeling language concerns the need of devising an appropriate syntax for the environment model. In STOCS and SCEL the point of contact with the environment is the knowledge base, which contains both internal information and externally-sensed events. In our approach, the knowledge is the most appropriate part of the language to specify environment models.

In summary, STOCS is essentially a modeling language which inherits the purpose and focus of SCEL. STOCS extends SCEL by modeling the average time duration of state-permanence and by replacing non-determinism by a probability distribution over outgoing transitions, thus adopting a CTMC-based operational semantics [5]. In the current phase of the design of STOCS, we deliberately omit to incorporate certain advanced features of SCEL, such as the presence and role of policies. In the same vein, we limited our investigation to a CTMC-based semantics at this stage, leaving for further study variants with a clear separation between stochastically timed actions and observable instantaneous actions, leading to a semantics based on IMCs or CTMDPs [10].

The outline of the paper is as follows. Section 3 discusses the trade-offs between four stochastic variants of SCEL, followed by the presentation of the key aspects of the formal semantics of two of them in Section 4. Section 5 introduces a case study to illustrate various aspects of the use of the design language in the context of a smart bike sharing system.

2 Related work

An overview of related work on a language-based approach to autonomic computing beyond the works cited in the introduction can be found in [7] and the references therein. For reasons of space limitations, here we restrict ourselves to mention a brief selection of directly relevant work that has not yet been addressed in the introduction. To the best of our knowledge there is no work available in the literature that addresses the stochastic extension of predicate based communication in the context of ensemble languages. There are a number of formal core languages that address dynamically changing network topologies in the context of mobile systems. This feature is directly relevant also to ensemble based systems. Examples are the calculus for wireless systems (CWS) proposed in [15] and the $\omega$-calculus [17], a calculus for mobile ad-hoc networks, which is a conservative extension of the $\pi$-calculus and which captures the ability of nodes to broadcast messages to other nodes that are within its physical transmission range. The calculus does not support general predicate-based communication and autonomic aspects of components.
3 STOCS: a Stochastic extension of SCEL

SCEL (Software Component Ensemble Language) [7] is a kernel language that takes a holistic approach to programming autonomic computing systems and aims at providing programmers with a complete set of linguistic abstractions for programming the behavior of Autonomic Components (ACs) and the formation of Autonomic Component Ensables (ACEs), and for controlling the interaction among different ACs. A SCEL program consists of a set of components of the form $I[K, P]$. Each component provides: a knowledge repository $K$, an interface $I$, and a process $P$.

The knowledge repository $K$ manages both application data and awareness data. Application data is used for enabling the progress of ACs’ computations, while awareness data provides information about the environment in which the ACs are running (e.g. monitored data from sensors) or about the status of an AC (e.g. its current location). The definition of SCEL abstracts from a specific implementation of knowledge repository. It is only assumed that there are specific operations for adding knowledge items in a repository ($K \oplus t$), for removing elements from a repository ($K \ominus T$), and for inferring elements from a repository ($K \vdash T$). In the sequel we let $\mathbb{V}$ denote the set of values, $\mathbb{K}$ denote the set of possible knowledge states, $\mathbb{I}$ denote the set of knowledge items, $\mathbb{T}$ denote the set of knowledge templates. The latter are used to retrieve data from the knowledge repository.

The component interface $I$ is used to publish and to make available structural and behavioral information about the component in the form of attributes, i.e. names acting as references to information stored in the component’s knowledge repository. Let $\mathbb{A}$ be the set of attribute names (which include the constant id used to indicate the component identifier); an interface $I$ is a function in the set $\mathbb{K} \rightarrow (\mathbb{A} \rightarrow \mathbb{V})$. An interface defines a (partial) function from a pair knowledge-base and attribute-name to the domain of values. Among the possible attributes, id is mandatory and is bound to the name of the component. Component names are not required to be unique, so that replicated service components can be modeled. The evaluation of an interface $I$ in a knowledge state $K$ is denoted as $I(K)$. The set of possible interface evaluations is denoted by $\mathbb{E}$.

A process $P$, together with a set of process definitions, can be dynamically activated. Some of the processes in $P$ execute local computations, while others may coordinate interaction with the knowledge repository or perform adaptation and reconfiguration. Interaction is obtained by allowing ACs to access knowledge in the repositories of other ACs. Processes can perform three different kinds of ACTIONS: get($T$)@c, qry($T$)@c and put($t$)@c, used to act over shared knowledge repositories by, respectively, withdrawing, retrieving, and adding information items from/to the knowledge repository identified by $c$. We restrict targets $c$ to the distinguished variable self, that is used by processes to refer to the component hosting it, and to component predicates $p$, i.e. formulas on component attributes. A component $I[K, P]$ is identified by a predicate $p$ if $I(K) \models p$, that is, the interpretation defined by the evaluation of $I$ in the knowledge state $K$ is a model of the formula $p$. Note that here we are assuming a fixed interpretation for functions and predicate symbols that are not within the attributes ($\mathbb{A}$). E.g. battery < 3 is a possible predicate, where < and 3 have a fixed interpretation, while the value of battery depends on the specific component addressed.[6]

The syntax of STOCS, a Stochastic Extension of SCEL, is presented in Table[1] where the syntactic categories of the language are defined. The basic category defines PROCESSES, used to specify the order in which ACTIONS can be performed. Sets of processes are used to define the behavior of COMPONENTS, that are used to define SYSTEMS. ACTIONS operate on local or remote knowledge-bases and have a TARGET to determine which other components are involved in the action. As we

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1For the sake of notational simplicity, in the present paper we assume that predicate $p$ in process actions implicitly refers only to the other components, excluding the one where the process is in execution.
The semantics of SCEL does not consider any time related aspect of computation. More specifically, the execution of an action of the form \( \text{act}(T)@c.P \) (for \( \text{put}/\text{get}/\text{qry} \) actions) is described by a single transition of the underlying SCEL LTS semantics. In the system state reached by such a transition it is guaranteed that the process which executed the action is in its local state \( P \) and that the knowledge repositories of all components involved in the action execution have been modified accordingly. In particular, SCEL abstracts from details concerning: (1) when the execution of the action starts, (2) if \( c \) is a predicate \( p \), when the possible destination components are required to satisfy \( p \), and (3) when the process executing the action resumes execution (i.e. becomes \( P \)).

In the extension of SCEL with an explicit notion of (stochastic) time, the time-related issues mentioned above can be addressed at different levels of abstraction, reflecting different choices of details in modeling SCEL actions. In this section, we discuss and motivate several design choices of STOCSS. In order to obtain an underlying CTMC semantics, we model state residence times in a Markovian way. Therefore, whenever we indicate that an action has rate \( \lambda \), we mean that the duration of the action (or, equivalently, the state residence time before action execution) is modeled by a random variable (RV, in the sequel) with negative exponential distribution having rate \( \lambda \). Indeed, the actual residence-time depends also on other conflicting actions the process may be engaged in, and the resulting race-condition.

Depending on the degree of detail in modeling these aspects, we have four different semantics: network-oriented \((\text{NET-OR})\), action-oriented \((\text{ACT-OR})\), interaction-oriented \((\text{INT-OR})\), and activity-oriented \((\text{ACTIV-OR})\). These semantics have an increasing level of abstraction, facilitating the management of the complexity of the model according to the application of interest. In the remaining part of this section we briefly discuss these four variants of the stochastic semantics and their motivations. In Section 4 we will provide a detailed definition for the \text{ACT-OR} and \text{NET-OR} semantics of a substantial fragment of STOCSS. Their complete formalization can be found in \cite{[14]}.

**Network-oriented Semantics.** This semantics takes into account points (1)–(3) mentioned previously and provides the most detailed modeling among the four semantics, which entails that actions are non-atomic. Indeed, they are executed through several intermediate steps, each of which requires appropriate time duration modeling. In particular, \text{put} actions are realized in two steps: (1) an envelope preparation and shipping (one for each component in the system, other than the source), (2) en-
velope delivery, with its own delivery time, test of the truth value of the communication predicate, and update of the knowledge-state. Also the actions get/qry are realized in two steps: (1) initiation of the item retrieval by a source component by entering in a waiting state, (2) synchronization with a destination component and exchange of the retrieved item. Since actions are not executed atomically, their (partial) execution is interleaved with that of other actions executed in parallel.

**Action-oriented Semantics.** In this simplified semantics, an action of the form \(\text{act}(T)@c\) (for put/get/qry actions) is described by a single transition and has a state residence time provided by taking into account the source component interface, the target component interface, the cost of retrieved/transmitted knowledge item, and possibly other parameters. For example, this rate may take into account the components locations and different response times of components. Upon item retrieval (by a get/qry action), eligible components (in terms of predicate satisfaction and availability of requested item) are in a race for response, with rate assigned component-wise. The underlying stochastic semantics drives the outcome of the race, with appropriate weighting depending on the rates. Even if this semantics does not consider all the realistic aspects of predicate-based communication, it is simpler, it generates a smaller CTMC, and can be used in scenarios where actions average execution time does not depend on the number of components involved in the communication.

**Interaction-oriented Semantics.** This is based on the action-oriented semantics and distinguishes local and remote actions, by assuming that local actions are executed instantaneously. In some scenarios, local actions happen in a time-scale which is very different (usually much smaller) from that of remote actions. In these situations it is reasonable to consider as instantaneous the execution of local actions, which is the idea we realize in the definition of the \text{INT-OR} semantics. As a useful side effect of ignoring the duration of local actions, we obtain more concise models. This approximation can be considered as an approach to reducing multi-scale models to single-scale models. In the latter, the macro-scale of inter-component communication drives the execution of macro-actions. A similar idea is explored for Bio-PEPA models in [9] and used to abstract away from fast reactions in biochemical networks. There, under the so-called Quasi-Steady-State Assumption of the system, it is also defined a form of bisimilarity between the abstract and the concrete model. The assumption we make for defining this semantics is that each remote (stochastically timed) action is followed by a (possibly empty) sequence of local (probabilistic) actions. We ensure this assumption is satisfied by imposing syntactic restrictions on processes. Then, by realizing a form of maximal progress [11] we execute a timed action and all of its subsequent probabilistic actions in a single transition of the S\text{TOCS} LTS.

**Activity-oriented Semantics.** This semantics is very abstract and allows to explicitly declare as atomic an entire sequence of actions, by assigning to it an execution rate of the entire sequence. Since the execution of the sequence of actions is atomic, it allows no interleaving of other actions. As an interesting consequence of this, we have a significant reduction in the state-space of the system. This variant of the semantics is motivated by the fact that S\text{TOCS} only provides primitives for asynchronous communication. Synchronization, if needed, has to be encoded through a protocol using asynchronous communication primitives [16]. Whatever is the adopted semantics among the previous ones (for example, the Action-oriented semantics), the protocol execution for the synchronization action is interleaved with the execution of other actions. This leads to unclear dependencies of protocol execution times from the environment. The Activity-oriented semantics allows us to declare as atomic an entire sequence of actions and to assign a rate to it. More in general, the purpose of this semantics is to have a very high-level abstraction of the interaction mechanisms. This must be handled with care as potentially relevant system behaviors (and interleavings) may be no longer present in the model. Therefore, properties of the model are not necessarily satisfied also by the system.
4 Stochastic Semantics of SCEL

In this section we show how a stochastic semantics of SCEL can be formalised when time abstractions presented in the previous sections are considered. Due to lack of space, we cannot provide all the details for all the variants. For this reason we focus our attention to a significative fragment of the rules rendering the action- and network-oriented variants. All the details are reported in the Appendix. The interested reader is referred to [14] where the details of all the abstractions are presented.

In all of the four semantics, interface evaluations are used within the so-called rate function $\mathcal{R}: \mathbb{E} \times \text{Act} \times \mathbb{E} \rightarrow \mathbb{R}_{\geq 0}$, which defines the rates of actions depending on the interface evaluation of the source of the action, the action (where Act denotes the set of possible actions), and the interface evaluation of the destination. For this purpose, interface evaluations will be embedded within the transition labels to exchange information about source/destination components in a synchronization action. The rate function is not fixed but it is a parameter of the language. Considering interface evaluations in the rate functions, together with the executed action, allows us to keep into account, in the computation of actions rates, various aspects depending on the component state such as the position/distance, as well as other time-dependent parameters. We also assume to have a loss probability function $f_{\text{err}}: \mathbb{E} \times \text{Act} \times \mathbb{E} \rightarrow [0, 1]$ computing the probability of an error in message delivery.

In the semantics, we distinguish between output actions (those issued by a component) and input actions (those accepted by a component). To simplify the synchronization of input and output actions, we assume input actions are probabilistic, and output actions are stochastic, therefore their composition is directly performed through a multiplication.

4.1 Preliminaries

Operational semantics of STOCS is given in the FUTSSs style [6] and, in particular, using its Rate Transition Systems (RTS) instantiation [5]. We now briefly recall preliminary definitions and notations.

In RTSs a transition is a triple of the form $(P, \alpha, \mathcal{P})$, the first and second components of which are the source state and the transition label, as usual, and the third component $\mathcal{P}$ is the continuation function that associates a real non-negative value with each state $P'$. A non-zero value represents the rate of the exponential distribution characterizing the time needed for the execution of the action represented by $\alpha$, necessary to reach $P'$ from $P$ via the transition. Whenever $\mathcal{P}(P') = 0$, this means that $P'$ is not reachable from $P$ via $\alpha$. RTS continuation functions are equipped with a rich set of operations that help to define these functions over sets of processes, components, and systems. Below we show the definition of those functions that we use in this paper, after having recalled some basic notation, and we define them in an abstract way, with respect to a generic set $X$.

Let $\text{TF}(X, \mathbb{R}_{\geq 0})$ denote the set of total functions from $X$ to $\mathbb{R}_{\geq 0}$, and $\mathcal{F}, \mathcal{P}, \mathcal{D}, \mathcal{I}$ range over it. We define $\text{FTF}(X, \mathbb{R}_{\geq 0})$ as the subset of $\text{TF}(X, \mathbb{R}_{\geq 0})$ containing only functions with finite support: function $\mathcal{F}$ is an element of $\text{FTF}(X, \mathbb{R}_{\geq 0})$ if and only if there exists $\{d_1, \ldots, d_m\} \subseteq X$, the support of $\mathcal{F}$, such that $\mathcal{F} d_i \neq 0$ for $i = 1 \ldots m$ and $\mathcal{F} d = 0$ for all $d \in X \setminus \{d_1, \ldots, d_m\}$. We equip $\text{FTF}(X, \mathbb{R}_{\geq 0})$ with the operators defined below. The resulting algebraic structure of the set of finite support functions will be crucial for the compositional features of our approach.

**Def. 4.1** Let $X$ be a set, and $d, d_1, \ldots, d_m$ be distinct elements of $X$, $\gamma_1, \ldots, \gamma_m \in \mathbb{R}_{\geq 0}$, $\bullet: X \times X \rightarrow X$ be an injective binary operator, $\mathcal{F}_1$ and $\mathcal{F}_2$ in $\text{FTF}(X, \mathbb{R}_{\geq 0})$:

1. $[d_1 \mapsto \gamma_1, \ldots, d_m \mapsto \gamma_m]$ denotes the function associating $\gamma_i$ to $d_i$ and $0$ to the other elements; the $0$ constant function in $\text{FTF}(X, \mathbb{R}_{\geq 0})$ is denoted by $[]$;

2. Function $+$ is defined as $(\mathcal{F}_1 + \mathcal{F}_2)d =_{\text{def}} (\mathcal{F}_1d) + (\mathcal{F}_2d)$;
3. Function $(\mathcal{P}_1 \bullet \mathcal{P}_2)$ maps terms of the form $d_1 \bullet d_2$ to $(\mathcal{P}_1 d_1) \cdot (\mathcal{P}_2 d_2)$ and the other terms to 0;
4. The characteristic function $\mathcal{X} : X \rightarrow \text{FTF}(X, \mathbb{R}_{\geq 0})$ with $\mathcal{X} d \equiv_{\text{def}} \{d \mapsto 1\}$.

**Def. 4.2** An $A$-labelled Rate Transition System (RTS) is a tuple $(S, A, \mathbb{R}_{\geq 0}, \rightarrow)$ where $S$ and $A$ are countable, non-empty, sets of states and transition labels, respectively, and $\rightarrow \subseteq S \times A \times \text{FTF}(S, \mathbb{R}_{\geq 0})$ is the $A$-labelled transition relation.

### 4.2 Knowledge repositories in STOCS

In STOCS, like in SCEL, no specific knowledge repository is defined. A knowledge repository type is completely described by a tuple $(K, I, T, \oplus, \ominus, \vdash)$ where $K$ is the set of possible knowledge states (the variables $K$, $K_1$, ..., $K'$, ...range over $K$), $I$ is the set of knowledge items (the variables $t$, $t_1$, ..., $t'$, ...range over $I$) and $T$ is the set of knowledge templates (the variables $T$, $T_1$, ..., $T'$, ...range over $T$). Knowledge items have no variable, while knowledge templates have. We assume a partial function $\text{match} : T \times I \rightarrow \text{Subst}(I)$ (where $\text{Subst}(X)$ is the set of substitutions with range in $X$) and we denote as $\text{match}(T, t) = \nothing$ the substitution obtained by matching the pattern $T$ against the item $t$, if any. By a small abuse of notation, we write $\neg \text{match}(T, t)$ to denote that $\text{match}(T, t)$ is undefined.

The operators $\oplus$, $\ominus$, $\vdash$ are used to add, withdraw, and infer knowledge items to/from knowledge repositories in $K$, respectively. These functions have the following signature, where $\text{Dist}(X)$ denotes the class of probability distributions on a set $X$ with finite support:

- $\oplus : K \times I \rightarrow \text{Dist}(K)$,
- $\ominus : K \times T \leftarrow \text{Dist}(K \times I)$,
- $\vdash : K \times T \leftrightarrow \text{Dist}(I)$.

Function $\oplus$ is total and defines how a knowledge item can be inserted into a knowledge repository: $K \oplus t = \pi$ is the probability distribution over knowledge states obtained as the effect of adding $t$. If the item addition operation is modeled in a deterministic way, then the distribution $\pi$ is a Dirac function.

Function $\ominus$ is partial and computes the result of withdrawing a template from a knowledge state as a probability distribution $K \ominus T$ over all pairs $(K, t) \in (K \times I)$ such that the item $t$ matches the template $T$. Intuitively, if $K \ominus T = \pi$ and $\pi(K', t) = p$ then, when one tries to remove an item matching template $T$ from $K$, with probability $p$ item $t$ is obtained and the resulting knowledge state is $K'$. If a tuple matching template $T$ is not found in $K$ then $K \ominus T$ is undefined, which is indicated by $K \ominus T = \perp$.

Function $\vdash$ is partial and computes (similarly to $\ominus$) a probability distribution over the possible knowledge items matching template $T$ that can be inferred from $K$. Thus, if $K \vdash T = \pi$ and $\pi(t) = p$ then the probability of inferring $t$ when one tries to infer from $K$ a tuple matching $T$ is $p$. If no tuple matching $T$ can be inferred from $K$ then $K \vdash T$ is undefined, which is indicated by $K \vdash T = \perp$.

### 4.3 Action-oriented Operational Semantics

This variant of the STOCS operational semantics (called $\text{ACT-OR}$) is defined according to the classical principle adopted for the definition of stochastic variants of Process Algebras: the execution of each action takes time, which is modeled by a RV exponentially distributed according to a rate $\lambda$.

In this semantics the rate associated to an action depends on the type of action performed (e.g. $\text{put}$, $\text{get}$ or $\text{qry}$), on the knowledge item involved in the action and on the evaluation interfaces of the interacting components according to the rate function $\mathcal{R} : E \times \text{Act} \times E \rightarrow \mathbb{R}_{\geq 0}$ which takes the interface evaluation of the source, an action in the set of labels

$$\text{Act} = \{ \text{put}(t)@c, \text{get}(T : t)@c, \text{qry}(T : t)@c \mid t \in I \text{ and } T \in T \text{ and } c \in \text{TARGET} \}$$

and the interface evaluation of the destination, and returns a value in $\mathbb{R}_{\geq 0}$, which is the rate of execution of the given action with counterparts having those interface evaluations. Note that $\text{get/qry}$ action labels have argument $T : t$ (rather than $T$ as in Table 1) because the labels of the $\text{get/qry}$ transition will contain also the matching/retrieved term $t$. 

The first rule states that \( e \) is defined according to the grammar below (where \( e \) of process terms defined according to the syntax of S"): 

\[
\begin{align*}
\text{Inactive process:} & \\
\text{nil} & \xrightarrow{\alpha} \langle \text{NIL} \rangle
\end{align*}
\]

Actions (where, \( gq \in \{\text{get, qry}\} \) and \( c \) is a \text{TARG}ET):

\[
\begin{align*}
\lambda = \mathcal{R}(\sigma, \text{put}(t)@c, \_): \quad & (\text{PUT}) \\
\text{put}(t)@c.P & \quad \text{put}(t)@c.P \quad \text{PUT}_B
\end{align*}
\]

\[
\begin{align*}
\text{match}(T,t) = \emptyset: \quad & \lambda = \mathcal{R}(\sigma, gq(T:t)@c, \delta): \quad (\text{GQ}) \\
gq(T)@c.P & \quad \text{gq}(T)@c.P \quad \text{GQ}_B1
\end{align*}
\]

\[
\begin{align*}
\text{match}(T,t) & \quad \text{gq}(T)@c.P \quad \text{gq}(T)@c.P \quad \text{GQ}_B2
\end{align*}
\]

Choice, definition, and parallel composition:

\[
\begin{align*}
P & \xrightarrow{\alpha_e} \mathcal{P} \quad Q & \xrightarrow{\alpha_e} \mathcal{Q} \quad (\text{CHO}) & P & \xrightarrow{\alpha} \mathcal{P} \quad \mathcal{Q} & \xrightarrow{\alpha_e} \mathcal{Q} \quad (\text{DEF}) \\
P + Q & \xrightarrow{\alpha_e} \mathcal{P} + \mathcal{Q} \quad P & \xrightarrow{\alpha} \mathcal{P} \quad (\mathcal{Q}) & P & \xrightarrow{\alpha_e} \mathcal{P} \quad (\mathcal{Q}) & \quad \mathcal{P} \quad (\text{PAR})
\end{align*}
\]

Table 2: Operational semantics of STOC5 processes (\text{ACT-OR}).

### 4.3.1 Operational semantics of processes

The \text{ACT-OR} semantics of STOC5 \text{processes} is the RTS \((\text{Proc}, \text{Act}_{\text{Proc}}, \mathbb{R}_{\geq 0}, \xrightarrow{\varepsilon})\) where \text{Proc} is the set of process terms defined according to the syntax of STOC5 given in Table[1]. The set \text{Act}_{\text{Proc}} of labels is defined according to the grammar below (where \( e' \) is the evaluation of an interface, \( t \in \mathbb{I} \), \( T \in \mathbb{T} \), and \( c \) is a \text{TARG}ET).

\[
\text{Act}_{\text{Proc}} \quad ::= \quad \text{put}(t)@c \quad | \quad e': \text{get}(T:t)@c \quad | \quad e': \text{qry}(T:t)@c
\]

The transition relation \( \xrightarrow{\varepsilon} \subseteq \text{Proc} \times \text{Act}_{\text{Proc}} \times \text{FTF}(\text{Proc}, \mathbb{R}_{\geq 0}) \) is the least relation satisfying the rules of Table[7]. This relation describes how a process evolves when one of the STOC5 actions is executed and is parameterized by an interface evaluation \( e \) that is the one associated to the component where the process is running. In the rest of this paper, we will omit the parameter if unnecessary.

Rule (NIL) states that \text{nil} is the terminated process, since no process is reachable from it via any action. Rules (PUT) and (PUT\_B) describe possible transitions of a process of the form \text{put}(t)@c.P. The first rule states that \text{put}(t)@c.P evolves with rate \( \lambda \) to \( P \) after a transition labeled \text{put}(t)@c. This rate is computed by using rate function \( \mathcal{R} \). The execution of a \text{put}(t)@c action depends on the source component and all the other components in the system, which are involved as potential destinations. Consequently, the execution rate \( \lambda \) can be seen as a function of the action and of the source component (interface evaluation) only; in particular, the action rate does not depend on (the interface evaluation of) a specific (destination) component; this is represented by using the symbol _ in the destination argument of \( \mathcal{R} \). On the contrary, rule (PUT\_B) states that \text{put}(t)@c.P cannot reach any process after a
transition with a label that is different from $\text{put}(t) \oplus c$.

Rules (GQ), (GQB1) and (GQB2) are similar and describe the evolution of a process of the form $\text{gq}(T) \oplus c \cdot P$, where $\text{gq} \in \{\text{get.qry}\}$. In this case, a process is reachable from $\text{gq}(T) \oplus c \cdot P$ only after a transition labeled $\delta : \text{gq}(T : t) \oplus c$. The latter indicates a request for a knowledge item $t$ matching template $T$ from a component identified by $c$. Note that, in the case of $\text{gq}(T) \oplus c$ the execution rate depends also on the destination interface evaluation. This is because only one destination will be involved in the completion of the execution of the action. Rules (CHO), (DEF) and (PAR) are standard.

4.3.2 Operational semantics of components and systems

The stochastic behaviour of STOCS systems is defined by the RTS $(\text{Sys}, \text{ActSys}, \mathbb{R}_{\geq 0}, \rightarrow)$ where $\text{Sys}$ is the set of system terms defined according to the syntax of STOCS given in Table 1. The set $\text{ActSys}$ of labels consists of three groups of labels of the form $\mathcal{X}$, $\alpha$ and $\overline{\mathcal{X}}$ formally defined according to the grammar below (where $\text{gq} \in \{\text{get.qry}\}$, $e'$ is the evaluation of an interface, $t \in \mathbb{I}$, $T \in \mathbb{T}$, and $p$ is a $\text{PREDICATE}$):

$$\text{ActSys} ::= e' : \text{put}(t) \oplus p \mid e' : \text{gq}(T : t) \oplus p \mid (\text{input actions})$$

$$\overline{e'} : \text{put}(t) \oplus p \mid \overline{e'} : \text{gq}(T : t) \oplus p \mid (\text{output actions})$$

$$\overline{e'} : \text{put}(t) @ \text{self} \mid \overline{e'} : \text{gq}(T : t) @ c \mid (\text{synchronizations})$$

whereas $\rightarrow \subseteq \text{Sys} \times \text{ActSys} \times \text{FTF}(\text{Sys}, \mathbb{R}_{\geq 0})$. Due to lack of space, the complete definition of the transition relation is given in Appendix A. In Table 3 we present the rules governing the execution of $\text{put}$ actions at the level of components and systems.

<table>
<thead>
<tr>
<th>Rule</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\sigma = I(K)$, $\overline{\sigma : \text{put}(t) @ \text{self}}$, $\overline{\sigma : \text{put}(t) @ p}$</td>
<td>(C-PUTL) $K \oplus t = \pi$</td>
</tr>
<tr>
<td>$\overline{\sigma : \text{put}(t) @ \text{self}}$, $\overline{\sigma : \text{put}(t) @ p}$</td>
<td>(C-UTO) $I[K, P] \overrightarrow{\sigma : \text{put}(t) @ p} I[(\mathcal{X} K), \mathcal{P}]$</td>
</tr>
<tr>
<td>$\delta = I(K)$, $\overline{\delta \mid p : K \oplus t = \pi}$, $\overline{\text{perr} = f_{\text{err}}(\sigma, \overline{\text{put}(t) @ p}, \overline{\delta})}$</td>
<td>(C-PUT1) $I[K, P] \overrightarrow{\sigma : \text{put}(t) @ p} [I[K, P] \rightarrow \text{perr}] + I[\pi, (\mathcal{X} P)] \cdot (1 - \text{perr})$</td>
</tr>
<tr>
<td>$\overline{\sigma : \text{put}(t) @ p}$</td>
<td>(C-PUTIR) $I[K, P] \overrightarrow{\sigma : \text{put}(t) @ p} [I[K, P] \rightarrow 1]$</td>
</tr>
</tbody>
</table>

Table 1: Operational semantics of STOCS components, $\text{put}$ rules (ACT-OR).

Rule (C-PUTL) describes the execution of $\text{put}$ actions operating at self. Let $I[K, P]$ be a component; this rule states that $P$ executes action $\text{put}(t) @ \text{self}$ with local interface evaluation $\sigma = I(K)$ and evolves to $\mathcal{P}$, then a local execution of the action can occur and the entire component evolves with label $\overline{\sigma : \text{put}(t) @ \text{self}}$ to $I[\pi, \mathcal{P}]$, where $\pi = K \oplus t$ is a probability distribution over the possible knowledge states obtained from $K$ by adding the knowledge item $t$, while $I[\pi, \mathcal{P}]$ is the function which maps any term of the form $I[K, P]$ to $(\pi K) \cdot (\mathcal{P} P)$ and any other term to 0.
When the target of a put is not self but a predicate \( p \), rule (C-PUTO) is used. This rule simply lifts an output put action from the process level to the component level and transmits to its counterpart its current interface evaluation \( \sigma \) by including it in the transition label.

The fact that a component accepts a put is modelled via rules (C-PUTI) and (C-PUTIR). The first rule is applied when the component satisfies the predicate \( p \). When the predicate is not satisfied the second rule is applied. When predicate \( p \) is satisfied by \( I(K) \) and \( K \otimes t = \pi \), component \( I[K, P] \) accepts the put action and evolves to \( I(K, P) \rightarrow p_{err} \). The first term, that is selected with probability \( p_{err} \), models a failure in the action execution, for instance due to a communication error. Value \( p_{err} \) is computed by the function \( f_{err} \) taking into account the source, the action performed, and the destination. The second term identifies the different configurations the component can reach when knowledge item \( t \) is added to the knowledge repository \( K \). Finally, if \( p \) is not satisfied by \( I(K) \), the component accepts an input put action producing no effect.

It is worth noting that rules (C-PUTI) and (C-PUTIR) deal with probability only. In fact, the actual rate of the action is the one which will result from system synchronization (Rules (S-PO) and (S-PI) in Table 4 on the basis of the rates settled by the rule (PUT) of Table 7.

Rule (S-PO) ensures that if any subsystem executes an output put action (i.e. a \( \sigma : \text{put}(t)@p \) labeled transition), the remaining subsystem must execute the corresponding input put action (i.e. a \( \sigma : \text{put}(t)@p \) labeled transition); the composed system does not exhibit a synchronization label, but it rather propagates the output \( \sigma : \text{put}(t)@p \) to allow further synchronization with all the other components in parallel; in the computation of the final rate it is necessary to consider output on the left sub-system and input on the right as well as the symmetric case.

Rule (S-PI) ensures that all subcomponents of a system synchronize, all together, on a (specific) input put action, completing the broadcast communication. Note that each component is constantly enabled on the input label for any put action (rules (C-PUTI) and (C-PUTO)).

### 4.4 Network-oriented Operational Semantics

The Action-oriented operational semantics considered in the previous section completely abstracts from the network structure and topology underlying a given STOCs specification. To make explicit the relevant interactions occurring when one-to-many SCel communications are performed, we introduce Network-oriented operational semantics (called NET-OR).

Let us consider a process \( P \), of the form \( \text{put}(v)@p.Q \), and the execution of action \( \text{put}(v)@p \), as illustrated in Figure 1. If we consider all the interactions occurring at the network level, the execution of this action begins with the creation of an envelope message that is shipped, typically in broadcast, to all the system components. After this message is shipped, \( P \) can proceed behaving like \( Q \). We can assume that the time needed to send this message is exponentially distributed according to a rate \( \lambda \).
When this message is received by a component, the latter first checks if its interface satisfies $p$, and if so, it delivers $t$ in its knowledge repository. We can assume that the time it takes the envelope message to reach a component is exponentially distributed with rate $\mu$, which may depend on $t$ as well as other parameters like, e.g., the distance between the sender and the receiver component.

To model this complex interaction we extend the syntax of processes by adding the new term $\{t@p\}_\mu$. This term, that is not available at the user syntax level, identifies a pending request for a put$(t)@p$; the parameter $\mu$ models the rate for transmission, predicate evaluation and repository update as discussed previously. When the request is activated, satisfaction of predicate $p$ is checked and, in the positive case, knowledge item $t$ is added to the local knowledge repository.

Let us consider three components: $C_1 = I_1[K_1,P_1]$, $C_2 = I_2[K_2,P_2]$, and $C_3 = I_3[K_3,P_3]$ and assume process $P_1$ is defined as put$(v)@p,Q$ as described above. Note that different components may be in different locations. The interaction we illustrate starts with process $P_1$ executing the first phase of put$(v)@p$, i.e. creating two copies of the special message $\{v@p\}$, one for component $C_2$ and one for component $C_3$, and sending these messages. The time required for this phase (denoted in blue in the figure) is modeled by a rate $\lambda$. The time for each message to arrive at component $C_j$ ($j = 2,3$), be evaluated against $I_j(K_j)$ and possibly cause the update of $K_j$ is modeled by RVs with rates $\mu_j$ (in Figure 1 this is illustrated by two arrows). The delivery of the two messages fails with probability $err_2$ and $err_3$, respectively, and succeeds with their complement (see Figure 2). The execution of component $C_1$ restarts as soon as the copies of the messages are sent, without waiting for their arrival at the destination components (the red stripe in the figure illustrates the resumed execution of $C_1$). The evaluation of predicate $p$ is performed when the message arrives at the corresponding component so, for example, it may happen that $C_2$ satisfies $p$ at the time the message arrives (so $K_2$ is updated accordingly), while $C_3$ does not satisfy $p$ (thus leaving $K_3$ unchanged).

The operational semantics of processes already presented in Section 4.3.1 is extended with the rules in Table 5. These rules operate in combination with the new rules for components reported in Table 6. Rule (C-PUTI) models the initiation of the execution of action put$(t)@c$; it allows the reception of a put action, and it is responsible for the creation of the envelope (carrying the incoming message) thus modeling its travel towards that component parametrized by rate $\mu$. The fact that the envelope is in parallel with the process of the potential receiver component by no means should
be interpreted as the representation of the fact that the message reached the component; simply, the
association between the message and the component is represented by means of a parallel composition
term; in other words, the fact that a specific message is ‘addressed’ to a component is represented
syntactically by such a parallel composition; this action will be executed with rate \( \lambda \), computed using
the function \( \mathcal{R} \) depending on the interface evaluation of the source \( \sigma \) (i.e. the container component)
and the sent item \( t \). This is postulated by the rule (PUT) and realized at system level by the broadcast
rules of Table 4 that are part of the (NET-OR) semantics of the put operation. Rule (C-ENVA)/(C-
ENVR) realizes envelope delivery by specifying the conditions under which a component accepts or
refuses, respectively, an arriving envelope.

## 5 Case Study

We develop a model of a bike sharing service, where we assume a city with \( m \) parking stations,
each one with his location \( \ell_i \in \text{Loc} = \{\ell_1, \ldots, \ell_m\} \), a number of available bikes \( b_i \), and a number of
available parking slots \( s_i \) (for \( i = 1, \ldots, m \)). Parking stations are in one-to-one correspondence with
the set of possible locations, which should be considered as (disjoint) areas of influence in the city.
We also assume to have \( n \) users of the bike sharing service: at any time, each user is positioned in
one location and can be in one of the two states Pedestrian and Biker. In each of the two states, the
user moves around the city (with speed depending on the state) according to its preferences, modeled
by two probability transition matrices \( Q_b \) and \( Q_p \) of size \( m \times m \) for the biker and the pedestrian state,
respectively. Then, the user becomes a Biker or a Pedestrian by transitions named Borrow and Return.

A user in a location \( \ell \) can borrow (or return) a bike by issuing a request (e.g. by means of a
mobile phone application) to the bike sharing system for a parking with an available bike (or slot)
within a neighborhood of \( \ell \). The bike sharing system answers with the location of a parking station
having an available bike or an available parking slot, within a neighborhood of \( \ell \) specified by a
neighborhood condition \( \varphi_n(\ell, \ell') \) (modeling, for example, that a parking station \( \ell' \) is easily reachable
from \( \ell \)). This flexibility allows some control on which parking station is selected among those that
are in the neighborhood of the current user location (including itself), which can be used to re-balance
slot/bike availability by redirecting users to parking station that have many available bikes (or slots).
Re-balancing performed by users can help reducing the cost of bike reallocation by means of trucks.

A single user is represented as a component \( I_u[\text{K}_u, \text{P}_u] \), whose knowledge state \( \text{K}_u \) is an element
\( \langle s, \ell \rangle \) in \( \{b, p\} \times \text{Loc} \) denoting the user state (i.e. either being a pedestrian or a biker) and the user
location, and whose interface \( I_u \) which defines the predicates biker, pedestrian, and loc(\( \ell \)) as follows:
\( I_u(\langle b, \ell \rangle) \models \text{biker} \), \( I_u(\langle p, \ell \rangle) \models \text{pedestrian} \), and \( I_u(\langle s, \ell \rangle) \models \text{loc}(\ell) \), for every \( \ell \in \text{Loc} \) and \( s \in \{b, p\} \).
Let us summarize the role of the user knowledge operators, defined in Appendix C The \( \oplus \) operator
allows: to change state by \( \oplus(b) \) (change to biker state) and by \( \oplus(p) \) (change to pedestrian state),
and to move to a specified location \( \ell' \) by \( \oplus(\text{go}, \ell') \). The \( \ominus \) operator allows to move to a location

\[
\begin{align*}
\delta &= I(K) & \mu &= \mathcal{R}(\sigma, \{t@p\}, \delta) & p_{err} &= f_{err}(\sigma, \{t@p\}, \delta) \\
I[K, P] &\xrightarrow{\sigma;\text{put}(t}@p\}) I[K, P] \mapsto p_{err}, I[K, P][\{t@p\}] \mapsto (1 - p_{err}) \\
I[K, P] &\xrightarrow{\tau}@p I[\pi, \mathcal{P}] & I[K, P] &\xrightarrow{\tau}@p I[\pi, \mathcal{P}]
\end{align*}
\]

Table 6: Operational semantics of STOCS components, put rules (NET-OR).
knowledge state is a vector $b$ of reserved bikes (similar to that of a pedestrian, except for the fact it reserves the city and, then, leaves his bike in a parking station by executing the process Return the parking location $\ell$ from a parking station $P$ according to the average user behavior in the pedestrian state, by $\ominus(p_{next}, L)$. The latter is also returned as a binding for the variable $L$. The process Borrow first retrieves the current location $L$ then performs a bike reservation (bike_res) from a parking station $ID$ satisfying predicate near($L$). The actual rate of this action depends on available bikes: the higher is the number of available bikes, the higher is the execution rate. As an effect of this race condition, the $ID$ of the near station containing more bikes is received by the user with a higher probability than a near station with fewer bikes, causing a more balanced distribution of bikes in the system. When the parking lot is reserved, the user moves towards the parking stations. The rate of this action depends on the distance between the user and the parking station. After that process Borrow takes a bike; this operation is performed via a get action that decrements the bikes available and increments the slots available. Finally, the user status is updated to biker $b$. A biker moves around the city and, then, leaves his bike in a parking station by executing the process Return. Its behavior is similar to that of a pedestrian, except for the fact it reserves parking slots instead of bikes.

A parking station is represented as a component $I_p[K_p, nil]$ that has no behavior (it is passive). Its knowledge state is a vector $\langle b_{a}, b_{r}, s_{a}, s_{r}, \ell \rangle \in \mathbb{N} \times Loc$ denoting the number of available bikes ($b_{a}$), of reserved bikes ($b_{r}$), of available parking slots ($s_{a}$), and of reserved parking slots ($s_{r}$), as well as the parking location $\ell$. The parking station interface $I_p$ defines the predicates $loc(\ell)$ and $near(\ell)$ as follows: $I_p(\langle b_{a}, b_{r}, s_{a}, s_{r}, \ell \rangle) \models loc(\ell)$ and $I_p(\langle b_{a}, b_{r}, s_{a}, s_{r}, \ell \rangle) \models near(\ell')$ if $q_b(\ell, \ell')$ holds, for every $\ell, \ell' \in Loc$ and $b_{a}, b_{r}, s_{a}, s_{r} \in \mathbb{N}$ (see Appendix C).

An initial state of this model is a term
\[ \|_{i=1}^{m} (\langle I_u(\ell_i, p), P_u \rangle[k_i] \parallel I_p(\langle b_i, 0, s_i, 0, \ell_i \rangle, nil) ) \]
which denotes, for $i = 1, \ldots, m$: (i) $k_i$ pedestrians in locations $\ell_i$, and (ii) $b_i$ available bikes and $s_i$ available parking slots in parking station at location $\ell_i$. Note that the number of reserved bikes as well as the number of reserved slots is set to zero at the initial state of the system in every parking station. The overall number of bikes in the system is preserved by the knowledge-update rules.

Some simple simulation analyses of the considered system are reported in Figure 4. These simulations, based on action oriented semantics, have been performed with jRESP\(^2\). This is a Java framework that can be used to execute and simulate SCEL/STOCs specifications. Figure 4 compares the simula-

![Figure 3: User behavior as a STOCS process.](http://jresp.sourceforge.org)
We can notice that the average number of available bikes in parking stations is similar in the two simulations. However, when the bikes/slots reservation rate depends on the available resources, the bikes are more evenly distributed over the different parking stations.

6 Conclusions and Future Work

We have introduced STOCs, a stochastic extension of SCEL, for the modeling and analysis of performance aspects of ensemble based autonomous systems. One of the original features of the language is the use of stochastic predicate based multi-cast communication which poses particular challenges concerning stochastically timed semantics. Four variants of the semantics, considering different levels of abstraction, have been discussed and for two of them the main aspects of the formal semantics have been provided. A case study concerning shared bikes systems was presented to illustrate the use of the various language primitives of STOCs.

The development of both numeric and statistical model-checking tools for STOCs is in progress and also the development of a fluid semantics and verification techniques to address large scale collective systems along the lines of work in [1,2] is planned as future work.

7 Acknowledgments

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References


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3We consider 40 users moving over a grid of $4 \times 4$ locations. Each parking station starts with 5 bikes and 5 empty slots.


A Action-oriented Operational Semantics

In this appendix we present all the details concerning the semantics called Action-oriented (abbreviated to ACT-OR), associating a single transition to each STOCS action. Then, in Appendix B we will describe the Network-oriented semantics (abbreviated to NET-OR) by showing only the necessary modifications to the ACT-OR semantics.

Before discussing the semantics in detail, we want to stress that not only interface evaluations are used in multicast communication to establish the truth value of predicates, but they are also used to compute appropriate action rates within the rate function \( \mathcal{R} \). Action labels are taken from the set \( \text{Act} = \{ \text{put}(t)@c, \text{get}(T:t)@c, \text{qry}(T:t)@c \mid t \in \mathbb{T} \text{ and } T \in \mathbb{T} \text{ and } c \in \text{TARGET} \} \). Note that get/qry actions argument has been set to \( T:t \) (rather than \( T \) as in Table [1]) because the labels of get/qry transition will contain also the matching/retrieved term \( t \). We do not explicitly give the definition of this function, as it is a parameter of the language. We plan, however, to extend the language with an appropriate syntax for defining the rate function in terms of sender/receiver component attributes and sent messages. Considering interface evaluations in the rate functions, together with the executed action, allow us to keep into account, in the computation of the action rate, various aspects depending on the component state such as the position/distance, as well as other time-dependent (i.e. knowledge state dependent) parameters such as the load of the component.

As discussed in Sec. [4] we also assume a loss probability function \( f_{\text{err}} : \mathbb{E} \times \text{Act} \times \mathbb{E} \to [0,1] \) that, similarly to the function \( \mathcal{R} \), computes the probability of an error in the delivery of messages. Also for this function we do not explicitly give the definition, as it is a parameter of the language, but we expect it to be defined through an appropriate syntax.

Interface evaluations, the rate function \( \mathcal{R} \), and the error function \( f_{\text{err}} \) have the roles described above also in the other semantics and we will avoid to mention them again in those sections.

A further clarification we want to make in this premise concerns synchronization of input and output actions. As mentioned in Sec. [3] an input action \( \alpha \) and an output action \( \tau \) synchronize into a \( \overrightarrow{\alpha} \) action. These synchronizations can happen within a component, for local actions (\( @\text{self} \)), between a source and a destination component, in remote get/qry actions (\( @p \)), and between a source component and all the remaining components, in remote put actions (\( @p \)). In the case of get/qry actions, the interface transmitted in the synchronization label will be that of the destination, which allows to have a different rate for each possible destination. In the case of put actions, the interface transmitted in the synchronization label will be that of the source, since all components are involved as destination (i.e. the rate cannot be affected by any specific destination component). Therefore, for the put action, we abstract from the actual destinations and we compute the rate only on the basis of the source.

A.1 Operational semantics of processes

In order to make this section self-contained, we recap here that the ACT-OR semantics of STOCS processes is the RTS \( (\text{Proc}, \text{Act}_{\text{Proc}}, \mathbb{R}_{\geq 0}, \rightarrow_e) \) where \( \text{Proc} \) is the set of process terms defined according to the syntax of STOCS given in Table [1]. The set \( \text{Act}_{\text{Proc}} \) of labels is defined according to the grammar below (where \( e' \) is the evaluation of an interface \( t \in \mathbb{T}, T \in \mathbb{T} \), and \( c \in \text{TARGET} \)) and it is ranged over by \( \alpha, \alpha', \ldots :$

\text{Act}_{\text{Proc}} := \text{put}(t)@c \mid e' : \text{get}(T : t)@c \mid e' : \text{qry}(T : t)@c

and \( \rightarrow_e \subseteq \text{Proc} \times \text{Act}_{\text{Proc}} \times \mathbb{FTF}(\text{Proc}, \mathbb{R}_{\geq 0}) \) is the least relation satisfying the rules of Table [7] which we describe in the rest of this section (\( \rightarrow_e \) is parameterized by an interface evaluation \( e \): we feel free to omit the parameter if unnecessary).
Inactive process:
\[
\text{nil} \xrightarrow{\alpha} \text{(NIL)}
\]

Actions (where, \(\text{gq} \in \{\text{get, qry}\}\) and \(c\) is a \text{TARGET}):
\[
\begin{align*}
\lambda &= \mathcal{R}(\sigma, \text{put}(t)@c, \_). \\
\text{put}(t)@c \cdot P \xrightarrow{\text{put}(t)@c} \sigma.P \xrightarrow{\lambda} (\text{PUT}) \\
\alpha &\neq \text{put}(t)@c \\
\text{put}(t)@c \cdot P &\xrightarrow{\alpha} [] (\text{PUT}B)
\end{align*}
\]
\[
\begin{align*}
\text{match}(T, t) &= \emptyset \\
\lambda &= \mathcal{R}(\sigma, \text{gq}(T : t)@c, \delta). \\
\text{gq}(T)@c \cdot P \xrightarrow{\delta \cdot \text{gq}(T : t)@c} \sigma. P \xrightarrow{\lambda} (\text{GQ}) \\
\alpha &\neq \text{gq}(T : t)@c \\
\text{gq}(T)@c \cdot P &\xrightarrow{\alpha} [] (\text{GQB1})
\end{align*}
\]
\[
\begin{align*}
\neg \text{match}(T, t) \\
\text{gq}(T)@c \cdot P &\xrightarrow{\text{gq}(T : t)@c} [\text{GQB2}]
\end{align*}
\]

Choice, definition, and parallel composition:
\[
\begin{align*}
P &\xrightarrow{\alpha_e} P Q \xrightarrow{\alpha_e} Q \\
P &\xrightarrow{\alpha_e} P + Q \xrightarrow{\alpha_e} P + Q \\
A(\overline{\mathcal{X}}) &\overset{\text{def}}{=} P \xrightarrow{\overline{\mathcal{V}}} Q \alpha_e P \xrightarrow{A(\overline{\mathcal{V}})} \alpha_e P \\
\alpha_e &\overset{\text{CHO}}{=} P + Q \alpha_e P + Q \\
\alpha_e &\overset{\text{DEF}}{=} P \alpha_e P + Q \alpha_e Q \\
P &\xrightarrow{\alpha_e} P | Q \alpha_e P | (\mathcal{X} Q) + (\mathcal{X} P) | Q \alpha_e P | Q \xrightarrow{\alpha_e} Q (\text{PAR})
\end{align*}
\]

Table 7: Operational semantics of STOCs processes (ACT-OR).

The rules in Table 7 have been illustrated in Section 4. Here we only add a remark concerning the rule \(\text{PAR}\): given two functions \(\mathcal{R}_1\) and \(\mathcal{R}_2\), the function \(\mathcal{R}_1 \mid \mathcal{R}_2\) applied to process term \(R\) returns the product \((\mathcal{R}_1 R_1) \cdot (\mathcal{R}_2 R_2)\), whenever \(R\) is of the form \(R_1 \mid R_2\), for some terms \(R_1\) and \(R_2\), and 0 otherwise. In the rule, also the characteristic function \(\mathcal{X}\) is used. Function \(\mathcal{R} \mid (\mathcal{X} Q)\) applied to \(R\) returns \(\mathcal{R} R'\) if \(R = R' \mid Q\) for some \(R'\) and 0 otherwise; i.e. the function behaves as the continuation \(\mathcal{R}\) of \(P\) for terms where \(Q\) does not progress (for one step). In conclusion, \(\mathcal{R} \mid (\mathcal{X} Q) + (\mathcal{X} P) \mid Q\) correctly represents process interleaving, keeping track of the relevant rates.

### A.2 Operational semantics of components and systems

We present the entire ACT-OR semantics of STOCs systems, defining the RTS \(\langle \text{sys}, \text{Act}_{\text{sys}}, \mathbb{R}_{\geq 0}, \rightarrow \rangle\) where \(\text{sys}\) is the set of system terms defined according to the syntax of STOCs given in Table 1. The set \(\text{Act}_{\text{sys}}\) of labels is defined according to the grammar below (where \(\text{gq} \in \{\text{get, qry}\}\), \(e'\) is the evaluation of an interface, \(t \in \mathbb{T}\), \(T \in \mathbb{T}\), and \(p\) is a \text{PREDICATE}):

\[
\begin{align*}
\text{Act}_{\text{sys}} &::= e' : \text{put}(t)@p \\
&\quad | e' : \text{gq}(T : t)@p \\
&\quad | (\text{input actions}) \\
e' \triangleright \text{put}(t)@p \\
&\quad | e' : \text{gq}(T : t)@p \\
&\quad | (\text{output actions}) \\
e' \triangleleft \text{put}(t)@self \\
&\quad | e' : \text{gq}(T : t)@c \\
&\quad | (\text{synchronizations})
\end{align*}
\]
where the process relation \( \mapsto \) (and \( \delta \) get \( C \- I \)) and, since the possible, in the execution of process \( P \) to be summed together considering all possibilities:

\[
\delta = I(K) \quad \delta \models p \quad K \oplus t = \pi \quad \delta \models p \quad K \oplus T = \pi \quad \delta \models p \quad K \oplus t = \pi
\]

\[
\delta = I(K) \quad \delta \models p \quad K \oplus T = \pi \quad \delta \models p \quad K \oplus t = \pi
\]

put actions:

\[
\begin{align*}
\sigma &= I(K) \quad P \xrightarrow{\text{put}(t)@self} \sigma \quad K \oplus t = \pi & \text{(C-PUTL)} \\
I[K, P] &\xrightarrow{\sigma \cdot \text{put}(t)@self} I[\pi(t), \mathcal{P}] \\
\sigma &= I(K) \quad P \xrightarrow{\text{put}(t)@p} \sigma \quad K \oplus t = \pi & \text{(C-PUTO)} \\
I[K, P] &\xrightarrow{\sigma \cdot \text{put}(t)@p} I[(\mathcal{X}K), \mathcal{P}] \\
\delta &= I(K) \quad \delta \models p \quad K \oplus t = \pi \quad \delta \models p \quad K \oplus T = \downarrow \quad \delta \models p \\ &\xrightarrow{\delta \cdot \text{get}(T)@p} I[K, P] \quad I[K, P] \xrightarrow{\sigma \cdot \text{get}(T)@self} I[\pi(t), \mathcal{P}] \quad I[K, P] \xrightarrow{\sigma \cdot \text{get}(T)@self} \emptyset \quad I[K, P] \xrightarrow{\sigma \cdot \text{get}(T)@self} \emptyset \quad I[K, P] \xrightarrow{\sigma \cdot \text{get}(T)@self} \emptyset \\
\delta &= I(K) \quad \delta \models p \quad K \oplus t = \pi \quad \delta \models p \quad K \oplus T = \downarrow \\
I[K, P] &\xrightarrow{\delta \cdot \text{get}(T)@p} I[\pi(t), \mathcal{X}P] \quad I[K, P] \xrightarrow{\delta \cdot \text{get}(T)@p} I[\pi(t), \mathcal{X}P] \quad I[K, P] \xrightarrow{\delta \cdot \text{get}(T)@p} I[\pi(t), \mathcal{X}P] \\
\delta &= I(K) \quad \delta \models p \quad K \oplus T = \pi \quad \delta \models p \quad K \oplus T = \downarrow \\
I[K, P] &\xrightarrow{\delta \cdot \text{get}(T)@p} I[K, P] \quad I[K, P] \xrightarrow{\delta \cdot \text{get}(T)@p} I[\pi(t)] \quad I[K, P] \xrightarrow{\delta \cdot \text{get}(T)@p} I[\pi(t)] \quad I[K, P] \xrightarrow{\delta \cdot \text{get}(T)@p} I[\pi(t)]
\end{align*}
\]

get/qry actions (where, \( gq \in \{\text{get, qry}\} \)):

\[
\begin{align*}
\sigma &= I(K) \quad P \xrightarrow{\text{get}(T)@self} \sigma \quad K \oplus T = \pi & \text{(C-GETL)} \\
I[K, P] &\xrightarrow{\sigma \cdot \text{get}(T)@self} I[\pi(t), \mathcal{P}] \\
\sigma &= I(K) \quad P \xrightarrow{\text{qry}(T)@self} \sigma \quad K \oplus T = \pi & \text{(C-QRYL)} \\
I[K, P] &\xrightarrow{\sigma \cdot \text{qry}(T)@self} I[(\mathcal{X}K) \cdot \pi(t), \mathcal{P}] \\
\sigma &= I(K) \quad P \xrightarrow{\delta \cdot \text{get}(T)@p} \sigma \quad K \oplus T = \pi & \text{(C-GQO)} \\
I[K, P] &\xrightarrow{\delta \cdot \text{get}(T)@p} I[K, \mathcal{P}] \\
\delta &= I(K) \quad \delta \models p \quad K \oplus T = \pi \quad \delta \models p \quad K \oplus T = \pi \quad \delta \models p \quad K \oplus T = \pi \\
I[K, P] &\xrightarrow{\delta \cdot \text{get}(T)@p} I[\pi(t), \mathcal{X}P] \quad I[K, P] \xrightarrow{\delta \cdot \text{get}(T)@p} I[\pi(t), \mathcal{X}P] \quad I[K, P] \xrightarrow{\delta \cdot \text{get}(T)@p} I[\pi(t), \mathcal{X}P] \\
\delta &= I(K) \quad \delta \models p \quad K \oplus T = \pi \\
I[K, P] &\xrightarrow{\delta \cdot \text{qry}(T)@p} I[K, P] \quad I[K, P] \xrightarrow{\delta \cdot \text{qry}(T)@p} I[\pi(t)] \quad I[K, P] \xrightarrow{\delta \cdot \text{qry}(T)@p} I[\pi(t)] \quad I[K, P] \xrightarrow{\delta \cdot \text{qry}(T)@p} I[\pi(t)]
\end{align*}
\]

Table 8: Operational semantics of STOCs components (ACT-OR).

and \( \rightarrow \subseteq Sys \times ActSys \times FTF(Sys, \mathbb{R}_\geq 0) \) is the least relation satisfying the rules of Tables 8 and 9, where the process relation \( \rightarrow_e \) defined in Table 7 is also used.

In Table 8 we present both the rules for the put action, already presented in Table 3 and the rules for get/qry actions, that are not present there. We now discuss the rules for get/qry actions.

(C-GETL)/(C-QRYL) realize the local get (qry) action retrieving an item \( t \in \mathbb{I} \) matching the pattern \( T \), if possible, in the execution of process \( P \) (in the label of the process action we include the item \( t \) and we include the interface evaluation \( \sigma \) of the component for computing the action rate) and, since the get (qry) action may result in several distinct knowledge bases, these need to be summed together considering all possibilities: \( \pi \) is a distribution over pairs (knowledge
base and knowledge item) and the possible components in the continuation are weighted by using \( \pi \);

(C-GQ0) lifts a get/qry output action to the level of the component, similarly to (C-PUTO), and produces a continuation computed by the \( \rightarrow \) relation (in rule GQ) using the source interface evaluation (\( \sigma \)) and the destination interface evaluation (\( \delta \), taken from the synchronization label);

(C-GETI)/(C-QRY1) under the condition that a component satisfies the predicate \( p \), allow the component to accept an input get (qry) action (respectively), by computing the continuation on the basis of the distribution \( \pi \) over possible pairs of knowledge state and retrieved item (retrieved item, respectively), computed by using the \( \ominus \) (\( \cdot \), respectively) operator, but they do not compute any rate as this is computed on the source side by rules (GQ/C-GQ0); notice that the component communicates its interface evaluation \( \delta \) (destination) in the synchronization label.

Concerning (C-PULTL), (C-PUT1), (C-GETL), and (C-GETI), put/get actions may result in several distinct knowledge states and the rate functions need to be summed together considering all possible knowledge states. This is addressed by using Def. 4.1 item (3) applied to the component syntactic constructor \( I[\cdot, \cdot] \), which is obviously injective. Thus, for \( \pi \in \text{Dist}(\mathbb{K}) \) and \( \mathcal{P} \in \text{FTF}(\text{Proc}, \mathbb{R}_{\geq 0}) \)

function \( I[\pi, \mathcal{P}] \in \text{FTF}(\text{Sys}, \mathbb{R}_{\geq 0}) \) returns \( (\mathcal{P} \pi) \cdot \pi(K) \) on systems \( I[K, P] \), for any \( P \), and 0 on any other system term. On the contrary, when we consider rules (C-QRYL) and (C-QRY1), even though qry may return several retrieved knowledge items, the actual transition fixes a precise item \( t \), whose retrieval probability \( \pi(t) \) is combined with the component continuation.

Let us now consider systems of components: similarly to | in the case of components, also the definition of the semantics of system parallel composition \( S_1 | S_2 \) uses Def. 4.1 item (3) applied to the system parallel composition syntactic constructor |, which is obviously injective. As usual, interleaving is modeled as a combination of lifted |, + on functions and the characteristic function.

In Table 9 we give the rules for systems, grouped by action type:

(S-PO)/(S-PI) realize the broadcast communication of put: (S-PO) ensures that if any subsystem executes an output put action (i.e. it executes a \( \sigma : \text{put}(i)@p \) labeled transition), then the remaining subsystem must execute the corresponding input put action (i.e. it should execute a \( \sigma : \text{put}(i)@p \) labeled transition); the composed system does not exhibit a synchronization label, but it rather propagates the output \( \sigma : \text{put}(i)@p \) to allow further synchronization with all the other components in parallel; in the computation of the final rate it is necessary to consider output on the left sub-system and input on the right as well as the symmetric case; while (S-PI) allows an input put action forcing all of the components of a sub-system to perform that action;

(S-GQS) realizes one-to-one synchronization of get/qry actions (which are not broadcast), denoted by a \( e : \text{gq}(T : i)@p \) label, and performs aggregation of: (1) the synchronization rate of the left (right) sub-system, with the right (resp. left) subsystem that must not progress (this is realized using the \( \mathcal{X} \) characteristic function), and (2) output rates of the left sub-system and input rates of the right subsystem (as well as the symmetric case), combined with the | operator;

(S-GQI) realizes the input get (resp. qry) action for systems in which one component, among those satisfying the target predicate and having a matching knowledge item, can answer;

(S-SPL/S-SGQL) allow a system to execute a local put/get/qry action and exposes the label denoting the type of action to allow appropriate aggregation of the observed rates.
**put** synchronization:

\[
\begin{align*}
S_1 \sigma: \text{put}(t)@p & \rightarrow J_1^o & S_1 \sigma: \text{put}(t)@p & \rightarrow J_1^i & S_2 \sigma: \text{put}(t)@p & \rightarrow J_2^o & S_2 \sigma: \text{put}(t)@p & \rightarrow J_2^i \\
S_1 \parallel S_2 \sigma: \text{put}(t)@p & \rightarrow J_1^o \parallel J_2^i & S_1 \parallel S_2 \sigma: \text{put}(t)@p & \rightarrow J_2^i \parallel J_2^o \\
S_1 \parallel S_2 \sigma: \text{put}(t)@p & \rightarrow J_1^i \parallel J_2^i & (S-PO)
\end{align*}
\]

**get/qry** synchronization (\(gq \in \{\text{get, qry}\})\):

\[
\begin{align*}
S_1 \delta: gq(T):@p & \rightarrow J_1^i & S_1 \delta: gq(T):@p & \rightarrow J_1^o & S_1 \delta: gq(T):@p & \rightarrow J_1^i & S_2 \delta: gq(T):@p & \rightarrow J_2^i \\
S_2 \delta: gq(T):@p & \rightarrow J_2^i & S_2 \delta: gq(T):@p & \rightarrow J_2^o & S_2 \delta: gq(T):@p & \rightarrow J_2^i & (S-GQS)
\end{align*}
\]

\[
\begin{align*}
S_1 \parallel S_2 \delta: gq(T):@p & \rightarrow J_1^i \parallel (X^o S_2) + J_1^o \parallel J_1^i \parallel J_2^o \parallel (X^o S_1) \parallel J_2^i \\
S_1 \parallel S_2 \delta: gq(T):@p & \rightarrow J_1^o \parallel (X^o S_2) + (X^o S_1) \parallel J_2^i & (S-GQI)
\end{align*}
\]

Internal actions (\(gq \in \{\text{get, qry}\})\):

\[
\begin{align*}
S_1 \leftarrow e: \text{put}(t)@self & \rightarrow J_1^i & S_2 \leftarrow e: \text{put}(t)@self & \rightarrow J_2^i & (S-SPL)
\end{align*}
\]

\[
\begin{align*}
S_1 \parallel S_2 \leftarrow e: \text{put}(t)@self & \rightarrow J_1^i \parallel (X^o S_2) + (X^o S_1) \parallel J_2^i \\
S_1 \parallel S_2 \leftarrow e: \text{put}(t)@self & \rightarrow J_1^i \parallel (X^o S_2) + (X^o S_1) \parallel J_2^i & (S-SGQL)
\end{align*}
\]

Table 9: Operational semantics of STOCS systems (ACT-OR).

### B Network-oriented Operational Semantics

For the sake of conciseness, in this section we illustrate only the modifications to the Action-oriented semantics necessary to model the Network-oriented semantics. In particular, in Tables [10, 11] and [12] we omit the rules that are unchanged w.r.t Tables [7, 8] and [9] and we just leave their label, as usual.

In order to realize this semantics we extend the set of labels of actions performed by processes and systems as described in the following.

#### B.1 Operational semantics of processes

The NET-OR semantics of STOCS processes is the RTS \((\text{Proc}, \text{Act}_\text{Proc}, \mathbb{R}_{\geq 0}, \rightarrow_e)\), where \(\text{Proc}\) is the set of process terms defined according to the syntax of STOCS given in Table [1] and the set \(\text{Act}_\text{Proc}\) of
Inactive process and envelopes:

\[
\text{(NIL, Table[7])} \quad \frac{\{t@p\}_\mu}{\text{env}_B} \quad \frac{\alpha \neq \{t@p\}}{\{t@p\}_\mu \alpha \rightarrow [\emptyset]}
\]

Actions (where, \(gq \in \{\text{get, qry}\}\), \(c\) is a TARGET, and \(p\) is a PREDICATE):

\[
\frac{\text{match}(T,t) = \emptyset}{\frac{\lambda = \cal R(\sigma,gq(T:t)@self,\_)}{gq(T)@self.P \xrightarrow{\sigma,gq(T:t)@self}_\sigma [P\emptyset \rightarrow \lambda]}} \quad \frac{\alpha \neq \cdot : gq(T:t)@self}{gq(T)@self.P \alpha \rightarrow [\emptyset]} \quad \text{(GQLB1)}
\]

\[
\frac{\neg \text{match}(T,t)}{\frac{\lambda = \cal R(\sigma,gq(T:t)@self,\_)}{gq(T)@self.P \xrightarrow{\cdot,gq(T:t)@self}_\sigma [\emptyset]}} \quad \alpha \neq \tau
\]

\[
\frac{\text{match}(T,t) = \emptyset}{\frac{\beta = \cal R(\sigma,\{gq(T:t)@p\},\delta)}{\{gq(T)@p\}.P \xrightarrow{\delta,(gq(T:t)@p)}_\sigma [P\emptyset \rightarrow \beta]}} \quad \frac{\alpha \neq \cdot : \{gq(T:t)@p\}}{\{gq(T)@p\}.P \alpha \rightarrow [\emptyset]} \quad \text{(GQDB1)}
\]

\[
\frac{\neg \text{match}(T,t)}{\{gq(T)@p\}.P \xrightarrow{\cdot,(gq(T:t)@p)}_\sigma [\emptyset]} \quad \alpha \neq \cdot : \{gq(T:t)@p\} \quad \text{(GQDB2)}
\]

Choice, definition, and parallel composition:

\[
\frac{\text{CHO, Table[7]}}{\{gq(T)@p\}.P \xrightarrow{\cdot,(gq(T:t)@p)}_\sigma [\emptyset]} \quad \text{(PAR, Table[7])}
\]

Table 10: Operational semantics of STOC\(S\) processes (NET-OR).

labels is defined according to the grammar below (where \(t \in \mathbb{T}, T \in \mathbb{T}, gq \in \{\text{get, qry}\}\), \(c\) is a TARGET, and \(e\) is the evaluation of an interface) and it is ranged over by \(\alpha, \alpha', \ldots\):

\[
\text{Act}_{\text{Proc}} ::= \tau \mid \{t@p\}_\mu \mid e : \text{put}(t)@c \mid e : gq(T:t)@c
\]

and \(\rightarrow \subseteq \text{Proc} \times \text{Act}_{\text{Proc}} \times \text{FTF}(\text{Proc}, \mathbb{R}_{\geq 0})\) is the least relation satisfying the rules of Table 10 (like in the ACT-OR semantics, \(\rightarrow_e\) is parametrized by \(e\), which is the interface evaluation of the component in which the process resides: we feel free to omit the parameter, if not used in the rule).

We now briefly illustrate the rules of Table 10. We assume to have additional syntactical terms (not available at the user syntax level) which we call envelopes. They are of the form \(\{t@p\}_\mu\), can be put in parallel with processes, and denote messages that are currently traveling towards targets. A second syntactical construct we introduce is \(\{\text{get}(T)@p\}\) (\(\{\text{qry}(T)@p\}\), respectively) which denotes a waiting state of the process and it is treated as an action.

(ENV) allows to complete envelope delivery within a duration parametrized by \(\mu\);
(PUT) allows a process to issue a put action at a target \(c\) with rate 1;
(GQL) allows a process to issue a \texttt{get(\texttt{qry}, respectively) action over the local knowledge repository (i.e. with target self). The rule models the execution of action \texttt{get}(T)@self \texttt{(\texttt{qry}(T)@self, respectively) by process \texttt{get}(T)@self.P \texttt{(\texttt{qry}(T)@self.P, respectively). The duration of this action is described by a rate $\lambda$ computed using the function $R$ depending on the interface evaluation of the source $\sigma$ (i.e. the container component) and on the action;

(GQW) realizes the first step of a \texttt{get(\texttt{qry}, respectively) action over a remote knowledge in a component satisfying a predicate $p$, which consists in preparing an envelope $\{\texttt{get}(T)@p\} \{\texttt{qry}(T)@p\}$, respectively), which takes a time interval exponentially distributed with rate $\lambda$, and brings process $P$ to a \textit{wait} state $\{\texttt{get}(T)@p\}.P \{\texttt{qry}(T)@p\}.P$, respectively). Recall that \texttt{get/qry} actions are \textit{blocking} and the execution of $P$ is resumed only when a counterpart satisfying $p$ has a knowledge item $t$ matching $T$ available and the delivery of $t$ is completed. The duration of this first step is described by a rate $\lambda$ computed using the function $R$ depending only on the interface evaluation of the source $\sigma$ (i.e. the container component) and the sent template $T$;

(GQD) realizes the second step of a \texttt{get(\texttt{qry}, respectively) action, which consists in the \textit{delivery} of the knowledge item $t$ matching $T$ and has a duration described by a rate $\beta$ computed by the function $R$. Note that in this case the function $R$ is computed considering interface evaluation of the source $\sigma$ and the destination $\delta$, as well as the sent item $t$, which means that this rate can be made dependent (for example) on the distance of the two parties.

B.2 Operational semantics of components and systems

The \textsc{net-or} semantics of \textsc{stocs} systems is the RTS $(\text{Sys}, \text{Act}_{\text{Sys}}, \mathbb{R}_{\geq 0}, \rightarrow)$, where $\text{Sys}$ is the set of system terms defined according to the syntax of \textsc{stocs} given in Table 1 and the set $\text{Act}_{\text{Sys}}$ of labels is defined according to the grammar below (where $\texttt{gq} \in \{\texttt{get, qry}\}$, $t \in \mathbb{T}$, $T \in \mathbb{T}$, $p$ is a \textsc{_predicate}, and $e$ is the evaluation of an interface):

$$\text{Act}_{\text{Sys}} ::= e : \text{put}(t)@p \mid e : \{\text{gq}(T : t)@p\} \mid (\text{input actions})$$

$$\tau \mid e : \{\text{gq}(T : t)@p\} \mid (\text{output actions})$$

$$(\text{envelopes})$$

and $\rightarrow \subseteq \text{Sys} \times \text{Act}_{\text{Sys}} \times \text{FTF(\text{Sys}, \mathbb{R}_{\geq 0})}$ is the least relation satisfying the rules of Tables 11 and 12 where the process relation defined in Table 10 is also used.

The definition of the semantics of system parallel composition $S_1 \parallel S_2$ uses Def. 4.1 item 3 applied to the system parallel composition constructor $\parallel$, which is injective. As usual, interleaving is modelled as a combination of lifted $\parallel$, $+$ on functions and the characteristic function. In the rules, we also use Def. 4.1 item 3 applied to the component syntactic constructors $I[\cdot, \cdot]$, which is injective.

In Table 11 rules are grouped to illustrate how the various action types are realized.

(C-PUTI) models the \textit{initiation} of the execution of action \texttt{put}(t)@c, which requires several steps to complete, it allows the reception of a \texttt{put} action, and it is responsible for the creation of the envelope (carrying the incoming message) in parallel to the local process of a component, thus modeling its travel towards that component in terms of the time necessary to reach it, parametrized by rate $\mu$ (the fact that the envelope is in parallel with the process of the potential receiver component by no means should be interpreted as the representation of the fact that the message reached the component; simply, the association between the message and the component is represented by means of a parallel composition term; in other words, the fact that a
put actions:

\[
\begin{align*}
\delta &= I(K) & \mu &= \mathcal{R}(\sigma, \{t \circ p\}, \delta) & p_{err} &= f_{err}(\sigma, \{t \circ p\}, \delta) \\
I[K, P] \xrightarrow{\sigma: \text{put}(t) \circ p} I[K, P] \implies p_{err}, & I[K, P][\{t \circ p\}] \mapsto (1 - p_{err}) \\
\end{align*}
\]

(C-PUTL, Table 8) (C-PUTO, Table 8) (C-PUT1)

get/qry actions (where, \(gq \in \{\text{get, qry}\}\)):

\[
\begin{align*}
\sigma &= I(K) & P \xrightarrow{\delta: \{\text{get}(T) \circ p\}} \pi & \mathcal{P} \\
I[K, P] \xrightarrow{\delta: \{\text{get}(T) \circ p\}} I[(\mathcal{P} K), \mathcal{P}] & \end{align*}
\]

(C-GQO) (C-GETL, Table 8) (C-QRYL, Table 8) (C-GETLB, Table 8) (C-QRYLB, Table 8)

\[
\begin{align*}
\delta &= I(K) & \delta \vdash p & K \circ t = \pi \\
I[K, P] \xrightarrow{\delta: \{\text{get}(T) \circ p\}} I[\pi(t), (\mathcal{P} P)] & \end{align*}
\]

(C-GET1) (C-GETLB1)

\[
\begin{align*}
\delta &= I(K) & \delta \vdash p & K \vdash T = \top \\
I[K, P] \xrightarrow{- \{\text{get}(T) \circ p\}} & \end{align*}
\]

(C-QRY1) (C-QRYLB1)

\[
\begin{align*}
\delta &= I(K) & \delta \vdash p & K \vdash T = \top \\
I[K, P] \xrightarrow{\delta: \{\text{qry}(T) \circ p\}} & \end{align*}
\]

(C-GETI) (C-QRYI)

\[
\begin{align*}
\delta &= I(K) & \delta \vdash p & K \vdash T = \top \\
I[K, P] \xrightarrow{- \{\text{qry}(T) \circ p\}} & \end{align*}
\]

\tau actions:

\[
\begin{align*}
\rho &= I(K) & P \xrightarrow{\tau \circ p} \mathcal{P} \end{align*}
\]

(C-TAU)

Table 11: Operational semantics of STOCs components (NET-OR).

Specific message is ‘addressed’ to a component is represented syntactically by such a parallel composition; this action is executed with rate \(\lambda\), computed using the function \(\mathcal{R}\) depending on the interface evaluation of the source \(\sigma\) (i.e. the container component) and the sent item \(t\); this is postulated by the rule (PUT) and realized at system level by the broadcast rules of Table 4.

(C-ENVA)/(C-ENVR) realize envelope delivery by specifying the conditions under which a component accepts or refuses, respectively, an arriving envelope;

(C-GQO) realizes an output get/qry action as in the ACT-OR semantics, but with a different label \(\{\ldots\}\) which denotes the synchronization on a waiting state;

(C-GETI)/(C-QRYI) realize an input get/qry action, again as in the ACT-OR semantics, but with a different label \(\{\ldots\}\);

(C-TAU) allows a component to make a \(\tau\) whenever its process makes such an action.
C Knowledge behavior and Rate Function (User/Parking Station)

In this section we describe the behavior of the user, given in Figure 3, in more detail. In particular, we describe the knowledge operators, defined by rules in Figure 5, and the actions rates, defined by cases in Figure 6. In this example we assume that message transmission is free of errors, that is \( f_{err}(\sigma, \alpha, \delta) = 0 \) for any interface evaluations \( \sigma, \delta \) and action \( \alpha \).

The user starts in the state Pedestrian, where movement is possible through a local get of the item \( p_{\text{next}} \). The choice of the location is resolved internally using the probability matrix \( Q_{\theta} \), as shown in the knowledge rule \( \text{KR}_4^u \). The effect of the action is the change of location of the user into \( \ell_j \), which is also returned as a binding for the variable \( L \). Note that the template is \( T = (p_{\text{next}}, L) \) and the retrieved item is \( t = (p_{\text{next}}, \ell_j) \). The location \( \ell_j \) is used to compute the rate of the action (i.e., of the movement), as shown in the definition \( \text{RR}_3^u \), specifying the rate function for this specific action.

The process Borrow retrieves the current location \( L \) (using rule \( \text{KR}_6^u \) and a rate given by \( \text{RR}_2^u \)). Then, it performs a bike reservation (\( \text{bike}_{\text{res}} \)) from a parking station ID satisfying predicate near(\( L \)): this triggers on the side of the parking station a knowledge action that decrements the number of available bikes, increments the number of reserved bikes, and returns the id of the selected parking station (by using rule \( \text{KR}_2^l \) and with rate \( \text{RR}_2^u \)). Here the template is \( T = (\text{bike}_{\text{res}}, L) \) and the retrieved item is \( t = (\text{bike}_{\text{res}}, \ell_i) \), which produces the binding \( L \mapsto \ell_i \). Note that the actual rate of this action depends on available bikes: the higher is the number of available bikes, the higher is the execution rate.

When the parking lot is reserved, the user goes to the parking station (which modifies the knowledge state according to \( \text{KR}_4^u \)). The rate of this action depends on the distance between the user and the parking station and on the pedestrian/biker state of the user (according to \( \text{RR}_1^u \)). After moving, the user takes a bike: this operation is performed via a get action whose effect on the parking knowledge state is given by rule \( \text{KR}_4^u \), that decrements the bikes available and increments the slots available (the action has rate given by \( \text{RR}_2^u \)). Finally, the user status is updated to biker (using \( \text{KR}_1^u \) and with rate \( \text{RR}_2^u \)).
Local actions:

\[
\begin{align*}
\text{RR}_a^u : \mathcal{R}(\sigma, \text{put}(\text{go}, \ell')@\text{self}, \sigma) &= \left\{ \begin{array}{ll}
\lambda_b \cdot f_{\text{dist}}(\ell, \ell') & \text{if } \sigma \models \text{biker} \land \text{loc}(\ell) \\
\lambda_p \cdot f_{\text{dist}}(\ell, \ell') & \text{if } \sigma \models \text{pedestrian} \land \text{loc}(\ell)
\end{array} \right. \\
\text{RR}_a^r : \mathcal{R}(\sigma, \text{put}(\text{p})@\text{self}, \sigma) &= \mathcal{R}(\sigma, \text{put}(\text{b})@\sigma) = \lambda_{\text{fast}} \\
\text{RR}_a^s : \mathcal{R}(\sigma, \text{get}((\text{p}, \text{next}, L):(\text{p}, \text{next}, \ell'))@\text{self}, \sigma) &= \lambda_p \cdot f_{\text{distance}}(\ell, \ell') \text{ if } \sigma \models \text{loc}(\ell) \\
\text{RR}_a^i : \mathcal{R}(\sigma, \text{get}((\text{b}, \text{next}, L):(\text{b}, \text{next}, \ell'))@\text{self}, \sigma) &= \lambda_b \cdot f_{\text{distance}}(\ell, \ell') \text{ if } \sigma \models \text{loc}(\ell) \\
\text{RR}_a^g : \mathcal{R}(\sigma, \text{qry}((\text{loc}, L):((\text{loc}, \ell'))@\text{self}, \sigma) &= \lambda_{\text{fast}}
\end{align*}
\]

Remote actions:

\[
\begin{align*}
\text{RR}_b^u : \mathcal{R}(\sigma, \text{put}(\text{bike})@\text{loc}(\ell), \delta) &= \mathcal{R}(\sigma, \text{get}(\text{bike})@\text{loc}(\ell), \delta) = \lambda_{\text{park}} \\
\text{RR}_b^r : \mathcal{R}(\sigma, \text{get}((\text{bike}, \text{res}, L):(\text{bike}, \text{res}, \ell'))@\text{near}(\ell), \delta) &= \frac{b_d}{b_a+s_a} \text{ if } \delta \models (\text{bikes} = b_a) \land (\text{slots} = s_a) \\
\text{RR}_b^s : \mathcal{R}(\sigma, \text{get}((\text{slot}, \text{res}, L):(\text{slot}, \text{res}, \ell'))@\text{near}(\ell), \delta) &= \frac{s_d}{s_a+s_a} \text{ if } \delta \models (\text{bikes} = b_a) \land (\text{slots} = s_a)
\end{align*}
\]

Figure 6: Rate Function, for any \( \ell, \ell' \in \text{Loc} \) and \( b_a, b_r, s_a, s_r \in \mathbb{N} \).

Bikers move around the city and, then, leave their bikes in a parking station by executing the process Return. Their behavior is similar to that of pedestrians, except for the fact that they perform complementary operations: they use a local get of the item b_next for moving (see rule RR_1^r and definition RR_1^i) instead of p_next, they perform a slot reservation slot_res (using rule RR_1^i and definition RR_1^i) instead of a bike reservation bike_res, and they return a bike to a parking station using a put action, rather than a get action (using rule RR_1^r and definition RR_1^i). After these actions, they return in state Pedestrian (using RR_1^i and with rate RR_1^i).

A fully specified model is obtained by fixing the parameters (all of them in \( \mathbb{R}_{\geq 0} \)): \( \lambda_{\text{fast}} \) denoting a fast rate for internal update actions, \( \lambda_{\text{park}} \) denoting a (uniform) interaction rate with the parking (e.g. locking/unlocking the bike), \( \lambda_p \) denoting the rate of movement of a pedestrian, and \( \lambda_b \) denoting the rate of movement of a biker, and also a distance function \( f_{\text{dist}} : \text{Loc} \times \text{Loc} \to \mathbb{R}_{\geq 0} \) that encodes the
connection topology of the locations. By giving concrete values to those parameters, to populations, and to bikes/slots in the initial state we obtain a finite state CTMC model for the described system.